# Crystallization and Structural Characterization of Two Europium Molybdates, $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ 

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#### Abstract

Crystals of two new europium molybdates, $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$, were grown in a melt of $\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 6.1-6.5 \mathrm{MoO}_{3}$ obtained by thermal decomposition of $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right]$. $6 \mathrm{H}_{2} \mathrm{O}$ or firing of the $\mathrm{Eu}_{2} \mathrm{O}_{3}+8 \mathrm{MoO}_{3}$ mixture at $800^{\circ} \mathrm{C}$ for 2 h in air. Repeated uses of reaction containers are effective in the crystallization. $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ crystallized in monoclinic, $C 2 / c$ (No. 15), $a=23.031(1), b=14.720(1), c=14.4097$ (7) $\AA$, $\beta=105.174(2)^{\circ}, \quad V=4714.8(4) \AA^{3}, \quad Z=8, \quad R_{1}=0.035, \quad$ and $\boldsymbol{w R}_{2}=0.064 . \mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ is a layer compound consisting of $\left\{\mathrm{MoO}_{4}\right\}$ - and $\left\{\mathrm{Mo}_{3} \mathrm{O}_{11}\right\}$-containing layers parallel to the bc plane and interstitial Eu atoms. $\mathrm{Eu}_{6} \mathbf{M o}_{10} \mathrm{O}_{39}$ crystallized in monoclinic, $C 2 / c$ (No. 15), $a=12.3008(5), b=19.6596(9)$, and $c=13.7691(4) \AA, \quad \beta=100.8934(9)^{\circ}, \quad V=3269.8(2) \AA^{3}, \quad Z=4$, $R_{1}=0.036$, and $w R_{2}=0.101$. The structure of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ is constructed of three-dimensionally arranged $\left\{\mathrm{MoO}_{4}\right\}$ and $\left\{\mathrm{Mo}_{2} \mathrm{O}_{7}\right\}$ groups and Eu atoms, being closely related to the structure of $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$. In both compounds, Eu atoms achieve seven- or eight-fold coordination by O atoms ( $<2.7 \AA$ ), and two $\mathrm{EuO}_{n}$ polyhedra share their edges or faces with a short Eu $\cdots$ Eu separations ranging from $3.6297(8)$ to $3.7168(6) \AA$. (C) 2001 Academic Press


Key Words: rare-earth molybdates; europium molybdates; polyoxomolybdates; thermal decomposition; crystal structures.

## INTRODUCTION

Phase equilibria and crystal structures of a $R_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$ ( $R=$ rare earths) system have long been explored and several compounds attract interests as inorganic materials (1). Since the discovery (2) of ferroelectric and ferroelastic properties of a series of $R_{2}\left(\mathrm{MoO}_{4}\right)_{3}$ (especially for $\left.\mathrm{Gd}_{2}\left(\mathrm{MoO}_{4}\right)_{3}\right)$, much attention has been paid to their preparation method, crystal growth, polymorphology, phase transition, and application to optoelectronic devices (1). $R_{2} \mathrm{MoO}_{6}$-based compounds are also of interest because of their potent catalytic activities (3). Recent topics on rare-earth molybdates are

[^0]ionic conduction behavior of $\mathrm{La}_{2} \mathrm{Mo}_{2} \mathrm{O}_{9}$ and $R_{2}\left(\mathrm{MoO}_{4}\right)_{3}$, which exhibit fast oxide-ion $(4,5)$ and trivalent ion $\left(R^{3+}\right)(6)$ conductions, respectively. In contrast to these well-characterized materials, information on other rare-earth molybdates is rather poor. Of the rare-earth molybdates with $R_{2} \mathrm{O}_{3}: \mathrm{MoO}_{3}=1: 6,1: 4,1: 3,1: 2,2: 1,3: 1,3: 10,7: 8$, and $9: 4$ found in the phase equilibria (7), most of the structural studies have concentrated on $R_{2}\left(\mathrm{MoO}_{4}\right)_{3}(1: 3), R_{2} \mathrm{MoO}_{6}$ (1:1), and their polymorphs (1,3). In particular, very little is known about the $\mathrm{Eu}_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$ system (7).

The present study describes the crystal structures of two novel europium molybdates, $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ (2:7) and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}(3: 10)$, in which the former is a first observation in the $\mathrm{R}_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$ system. The latter stoichiometry has been reported as $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ (8), a structure of which is different but closely related to $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$. Both europium molybdates were found in a melt of a $800^{\circ} \mathrm{C}$-decomposed polyoxomolybdoeuropate, $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right]$. $6 \mathrm{H}_{2} \mathrm{O}(9)$, which consists of an inifinite $\gamma$-octamolybdate polymer $\left\{\left(\mathrm{Mo}_{8} \mathrm{O}_{27}\right)^{6-}\right\}_{\infty}$ attached by hexahydrated $\left[\mathrm{Eu}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ cations and lattice water molecules. It was found that the firing of a mixture of $\mathrm{Eu}_{2} \mathrm{O}_{3}$ and $\mathrm{MoO}_{3}$ in a $1: 8$ molar ratio at $800^{\circ} \mathrm{C}$ also produced $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$. However, these preparation methods are not always successful, frequently yielding no crystals in the melt. We also describe and discuss the formation and crystallization conditions of the two compounds.

## EXPERIMENTAL

## Materials and Reactions

All chemicals were of analytical grade and used without further purification. The $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ powder was synthesized according to the literature (9), and ground in an agate mortar. The firing of samples in air was carried out using a temperature-controlled electric furnace with a horizontally arranged cylindrical heater (diameter, 60 mm ; length, 300 mm ) and an inner quartz tube (diameter,


FIG. 1. Microscopic images of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ crystals obtained by firing (a) $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$, (b) $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}+\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$, (c) $\mathrm{Eu}_{2} \mathrm{O}_{3}+8 \mathrm{MoO}_{3}$, and (d) $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}+\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ at $800^{\circ} \mathrm{C}$ for 2 h . The crystals in (a) and (c) were obtained by reusing the same alumina containers (see text).

30 mm ; length, 860 mm ). Both ends of the tube were closed with rubber caps when heating. The samples were heated in a boat-shaped alumina container (width, 10 mm ; height, 10 mm ; length, 70 mm ). The sample position in the furnace was carefully selected so that the temperature error was within $\pm 5^{\circ} \mathrm{C}$.

## Preparation of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$

Placed in the boat, the $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ was inserted in the $800^{\circ} \mathrm{C}$-preheated furnace and kept at

TABLE 1
Crystallographic Data and Results for the Structural Analyses

| Compound | $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ | $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ |
| :---: | :---: | :---: |
| Formula weight | 1171.40 | 2495.14 |
| Temperature (K) | 173 | 173 |
| X-ray source | MoK $\alpha(0.71069$ ¢ $)$ | MoK $\alpha(0.71069$ ® $)$ |
| Crystal system | Monoclinic | Monoclinic |
| Space group (No.) | C2/c (No. 15) | C2/c (No. 15) |
| Unit cell dimensions | $a=23.031(1) \AA$ | $a=12.3008(5) \AA$ |
|  | $b=14.720(1) \AA$ | $b=19.6596(9) \AA$ |
|  | $c=14.4097(7) \AA$ | $c=13.7691(4) \AA$ |
|  | $\beta=105.174(2)^{\circ}$ | $\beta=100.8934(9)^{\circ}$ |
| Volume | 4714.8(4) $\AA^{3}$ | 3269.8(2) $\AA^{3}$ |
| Z | 8 | 4 |
| $D_{\text {calc }}$ | $4.822 \mathrm{~g} \mathrm{~cm}^{-3}$ | $5.068 \mathrm{~g} \mathrm{~cm}^{-3}$ |
| $\mu(\mathrm{MoK} \alpha)$ | $141.35 \mathrm{~cm}^{-1}$ | $150.97 \mathrm{~cm}^{-1}$ |
| $F(000)$ | 6096 | 4440 |
| Crystal size ( $\mathrm{mm}^{3}$ ) | $0.30 \times 0.08 \times 0.10$ | $0.10 \times 0.10 \times 0.08$ |
| Crystal color and habit | colorless, block | colorless, block |
| Diffractometer | Rigaku RAXIS-RAPID imaging plate | Rigaku RAXIS-RAPID imaging plate |
| Data collection Oscillation range | Oscillation method $\begin{gathered} \phi=0^{\circ}, \chi=45^{\circ}, \\ \omega=130^{\circ}-190^{\circ}, \\ \phi=180^{\circ}, \chi=45^{\circ}, \\ \omega=0^{\circ}-160^{\circ} \end{gathered}$ | Oscillation method $\begin{gathered} \phi=0^{\circ}, \chi=45^{\circ}, \\ \omega=130^{\circ}-190^{\circ}, \\ \phi=180^{\circ}, \chi=45^{\circ}, \\ \omega=0^{\circ}-160^{\circ} \end{gathered}$ |
| Oscillation width | $\Delta \omega=5^{\circ}$ | $\Delta \omega=5^{\circ}$ |
| Exposure | $1 \mathrm{~min} /{ }^{\circ}$ | $1 \mathrm{~min} /{ }^{\circ}$ |
| $2 \theta_{\text {max }}$ | $55^{\circ}$ | $55^{\circ}$ |
| Reflections |  |  |
| Total | 21822 | 15542 |
| Unique ( $R_{\text {int }}$ ) | 5615 (0.080) | 3733 (0.074) |
| Observed | $4467(I>2 \sigma(I))$ | 3309 ( $I$ > 2 $2(I)$ ) |
| Transmission factor | 0.1380-0.3228 | 01086-0.3259 |
| Minimizing quantity on LS | $\sum \mathrm{w}\left(F_{\mathrm{o}}^{2}-F_{\mathrm{c}}^{2}\right)^{2}$ | $\sum \mathrm{w}\left(F_{\mathrm{o}}^{2}-F_{\mathrm{c}}^{2}\right)^{2}$ |
| No. of variables | 343 | 249 |
| $R_{1}^{a}$, w $R_{2}^{b}$ | 0.035, 0.064 | 0.036, 0.101 |
| Maximum shift/error | 0.002 | 0.001 |
| Goodness of fit | 1.86 | 1.12 |
| $\Delta \rho_{\text {max }}$ | $\begin{aligned} & 1.74 \mathrm{e}^{-} \AA^{-3}(1.74 \AA \\ & \text { from Eu(3)) } \end{aligned}$ | $\begin{aligned} & 1.88 \mathrm{e}^{-} \AA^{-3}(0.92 \AA \\ & \text { from } \mathrm{Eu}(1)) \end{aligned}$ |
| $\Delta \rho_{\text {min }}$ | $\begin{aligned} & -7.23 \mathrm{e}^{-} \AA^{-3}(0.57 \AA \\ & \text { from } \operatorname{Eu}(4)) \end{aligned}$ | $\begin{aligned} & -5.78 \mathrm{e}^{-} \AA^{-3}(0.78 \AA \\ & \text { from } \operatorname{Eu}(3)) \end{aligned}$ |

[^1]TABLE 2
Positional and Displacement Parameters

| Atom | $x$ | $y$ | $z$ | $U_{\text {eq }}\left(\AA^{2}{ }^{2}\right)$ | Atom | $x$ | $y$ | $z$ | $U_{\text {eq }}\left(\AA^{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ |  |  |  |  |  | $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ |  |  |
| $\mathrm{Eu}(1)$ | 0.11468(1) | 0.94183(3) | 0.14515(2) | 0.00779(9) | $\mathrm{Eu}(1)$ | 0.62533(3) | $0.65578(2)$ | 0.64568(3) | 0.0083(1) |
| $\mathrm{Eu}(2)$ | $0.62224(1)$ | 0.80716(3) | $-0.06347(2)$ | $0.00758(9)$ | $\mathrm{Eu}(2)$ | 0.41330(3) | 0.64879(2) | 0.41452(3) | $0.0085(1)$ |
| $\mathrm{Eu}(3)$ | $0.61104(1)$ | 0.94064(3) | 0.14556(2) | $0.00774(9)$ | $\mathrm{Eu}(3)$ | 0.41260(3) | 0.94262(2) | 0.91610(3) | 0.0118(1) |
| $\mathrm{Eu}(4)$ | 0.38039(2) | 0.69446(3) | 0.06576(2) | 0.00851(9) | $\mathrm{Mo}(1)$ | 0.91343(7) | 0.65447(3) | 0.83972(5) | 0.0120(2) |
| $\mathrm{Mo}(1)$ | 0.25540(3) | 0.80150(5) | 0.16578(4) | 0.0080(1) | $\mathrm{Mo}(2)$ | 0.60343(5) | 0.78370(4) | 0.86136(4) | 0.0084(2) |
| $\mathrm{Mo}(2)$ | 0.23021(2) | 0.88062(5) | $0.38732(4)$ | 0.0088(1) | $\mathrm{Mo}(3)$ | 0.81461(6) | $0.50026(4)$ | 0.63939(5) | 0.0100(2) |
| Mo(3) | 0.23507(3) | 0.59812(5) | $0.29796(4)$ | 0.0087(1) | $\mathrm{Mo}(4)$ | 0.59434(6) | $0.52063(4)$ | 0.86154(5) | 0.0091(2) |
| $\mathrm{Mo}(4)$ | 0.56998(3) | 1.05418(5) | -0.10035(4) | 0.0080(1) | $\mathrm{Mo}(5)$ | 0.80586(6) | 0.80898(4) | 0.61804(5) | 0.0110(2) |
| Mo(5) | $-0.06871(3)$ | 0.95043(5) | 0.10161(4) | 0.0081(1) | $\mathrm{O}(1)$ | 0.8739(5) | 0.4967(3) | $0.7656(4)$ | 0.022(2) |
| Mo(6) | 0.06123(2) | 0.69609(5) | 0.14481(4) | 0.0079(1) | $\mathrm{O}(2)$ | $0.9209(5)$ | 0.4992(3) | 0.5664(4) | 0.019(2) |
| Mo(7) | $0.56198(3)$ | 0.69459(5) | 0.14559(4) | 0.0084(1) | $\mathrm{O}(3)$ | 0.8944(5) | 0.8305(3) | $0.5319(4)$ | 0.012(1) |
| $\mathrm{O}(1)$ | $0.5794(2)$ | $0.9753(4)$ | 0.2875(3) | $0.017(1)$ | $\mathrm{O}(4)$ | 1.0000 | 0.6238(4) | 0.7500 | 0.020(2) |
| $\mathrm{O}(2)$ | 0.5895(2) | $0.7851(4)$ | 0.0862(3) | 0.014(1) | $\mathrm{O}(5)$ | 0.7719(5) | 0.6477(3) | $0.7986(5)$ | 0.016(2) |
| $\mathrm{O}(3)$ | 0.5899(2) | $0.9548(4)$ | -0.0260(3) | 0.010(1) | $\mathrm{O}(6)$ | 0.6040(5) | 0.5560(3) | $0.7439(4)$ | 0.017(1) |
| $\mathrm{O}(4)$ | 0.6009(2) | $0.7924(4)$ | -0.2347(3) | 0.022(2) | $\mathrm{O}(7)$ | $0.5445(4)$ | 0.7209(3) | $0.9306(4)$ | 0.014(1) |
| $\mathrm{O}(5)$ | 0.6001(2) | $0.6536(4)$ | -0.0594(4) | 0.015(1) | $\mathrm{O}(8)$ | $0.7289(5)$ | 0.4952(3) | $0.9150(4)$ | 0.021(2) |
| $\mathrm{O}(6)$ | 0.1994(2) | 0.8794(4) | 0.2573(3) | 0.012(1) | $\mathrm{O}(9)$ | 0.6077(5) | 0.7513(3) | 0.7411(4) | $0.015(1)$ |
| $\mathrm{O}(7)$ | 0.3852(2) | 0.8492(4) | 0.0606(4) | 0.015(1) | $\mathrm{O}(10)$ | 0.5163(5) | 0.5533(3) | $0.3595(4)$ | 0.014(1) |
| $\mathrm{O}(8)$ | 0.3992(2) | $0.7004(5)$ | 0.2331(4) | 0.026(2) | $\mathrm{O}(11)$ | 0.4578(5) | 0.5850(3) | 0.5647(4) | 0.014(1) |
| $\mathrm{O}(9)$ | 0.0745(2) | 1.0880(4) | 0.1022(4) | 0.019(1) | $\mathrm{O}(12)$ | $0.7500(5)$ | 0.5777(3) | 0.6094(4) | 0.019(2) |
| $\mathrm{O}(10)$ | 0.0870(2) | $0.9738(5)$ | 0.2904(3) | 0.022(2) | $\mathrm{O}(13)$ | 0.7853(5) | 0.7217(3) | 0.6232(4) | 0.018(2) |
| $\mathrm{O}(11)$ | 0.0863(2) | $0.7872(4)$ | 0.0819(3) | 0.014(1) | $\mathrm{O}(14)$ | $0.5348(5)$ | 0.8623(3) | 0.8551(4) | $0.015(1)$ |
| $\mathrm{O}(12)$ | 0.1951(2) | $1.0475(4)$ | 0.1570(4) | 0.018(1) | $\mathrm{O}(15)$ | $0.4464(5)$ | 0.7616(4) | $0.3664(5)$ | 0.028(2) |
| $\mathrm{O}(13)$ | 0.0079(2) | 0.9337(4) | 0.1208(4) | 0.021(2) | $\mathrm{O}(16)$ | 0.2400(5) | 0.7018(3) | 0.4185(4) | 0.017(1) |
| $\mathrm{O}(14)$ | 0.2455(2) | $0.7164(4)$ | 0.2600(3) | 0.017(1) | $\mathrm{O}(17)$ | $0.3596(7)$ | 0.6606(3) | 0.2349(5) | 0.032(2) |
| $\mathrm{O}(15)$ | 0.7040(2) | $0.7152(4)$ | -0.0661(4) | 0.016(1) | $\mathrm{O}(18)$ | 0.2810(5) | 0.5655(3) | $0.3874(5)$ | 0.023(2) |
| $\mathrm{O}(16)$ | 0.6955(2) | $0.9029(4)$ | -0.1156(4) | 0.018(1) | $\mathrm{O}(19)$ | 0.6778(6) | 0.8449(3) | $0.5751(6)$ | 0.026(2) |
| $\mathrm{O}(17)$ | 0.5158(2) | $0.7978(4)$ | -0.1290(4) | 0.020(1) | $\mathrm{O}(20)$ | 0.9533(6) | 0.6090(4) | 0.9468(4) | 0.028(2) |
| $\mathrm{O}(18)$ | 0.6885(2) | 0.8738(4) | 0.0812(3) | 0.012(1) |  |  |  |  |  |
| $\mathrm{O}(19)$ | 0.5048(2) | 0.9174(4) | 0.1113(3) | 0.017(1) |  |  |  |  |  |
| $\mathrm{O}(20)$ | $0.5770(2)$ | $1.0892(4)$ | 0.1031(3) | 0.019(1) |  |  |  |  |  |
| $\mathrm{O}(21)$ | 0.4847(2) | 0.7069(4) | 0.1294(4) | 0.021(1) |  |  |  |  |  |
| $\mathrm{O}(22)$ | $0.6957(2)$ | 1.0392(4) | 0.1977(4) | 0.019(1) |  |  |  |  |  |
| $\mathrm{O}(23)$ | 0.6875(2) | 0.8764(4) | 0.2856(4) | 0.017(1) |  |  |  |  |  |
| $\mathrm{O}(24)$ | 0.2857(2) | 0.7282(4) | 0.0975 (3) | 0.014(1) |  |  |  |  |  |
| $\mathrm{O}(25)$ | 0.1944(2) | 0.8493(4) | 0.0782(3) | $0.015(1)$ |  |  |  |  |  |
| $\mathrm{O}(26)$ | 0.0931(1) | $0.9506(4)$ | -0.0242(3) | 0.010(1) |  |  |  |  |  |
| $\mathrm{O}(27)$ | 0.2052(2) | $0.9763(4)$ | 0.4308(4) | 0.022(2) |  |  |  |  |  |

$800^{\circ} \mathrm{C}$ for 2 h after a recovery of the temperature. The sample was then quenched by exposure to ambient temperature. Colorless crystals of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ (often together with $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ ) were formed in a gray-brown glassy melt of $\mathrm{Eu}_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$. However, the crystallization of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ was not always successful: one could find no crystals in the melt especially when the virgin alumina container was used. We found that repeated uses of the same container were effective in improving the crystallization properties. Figure 1a shows a photograph of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ obtained when the boat was reused three times. When the container was reused, the previous sample was removed from the container only mechanically, without further washing or chemical treatment. A firing $\left(800^{\circ} \mathrm{C}, 2 \mathrm{~h}\right)$ of the
$\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ obtained as seed crystals covered with $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ powders ( 20 mg ) yielded well-formed large $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ crystals (Fig. 1b). It should be noted that the addition of too much $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ resulted in a dissolution of the seed crystals to the melt.

We found that heating a $\mathrm{Eu}_{2} \mathrm{O}_{3}: \mathrm{MoO}_{3}=1: 8$ mixture (same Eu:Mo ratio as $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ ) under the same conditions yielded $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ crystals in a gray-brown melt of $\mathrm{Eu}_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$. Also in this case, repeated uses of the same alumina container were effective in the crystallization. Figure 1c shows a $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ crystal (together with $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ ) formed in a container that was reused five times. IR spectrum: $977.7 \mathrm{~m}, 950.7 \mathrm{~s}, 939.2 \mathrm{~s}(\mathrm{sh})$,

TABLE 3
Selected Interatomic Distances ( $\AA$ )

| $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ |  |  |  |  |  | $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Eu(1) | $\mathrm{O}(9)$ | 2.359(6) | Mo(1) | $\mathrm{O}(23)^{\text {ii }}$ | $1.719(5)$ | Eu(1) | $\mathrm{O}(12)$ | 2.290(6) | $\mathrm{Mo}(1)$ | $\mathrm{O}(20)$ | 1.715(6) |
|  | $\mathrm{O}(26)$ | 2.364(4) |  | $\mathrm{O}(24)$ | $1.726(5)$ |  | $\mathrm{O}(9)$ | 2.326 (5) |  | $\mathrm{O}(15)^{\mathrm{vii}}$ | 1.721(7) |
|  | $\mathrm{O}(6)$ | $2.369(5)$ |  | $\mathrm{O}(25)$ | $1.769(5)$ |  | $\mathrm{O}(13)$ | 2.424(6) |  | $\mathrm{O}(5)$ | 1.731(7) |
|  | $\mathrm{O}(10)$ | $2.389(5)$ |  | $\mathrm{O}(14)$ | 1.904(5) |  | $\mathrm{O}(6)$ | 2.425(6) |  | $\mathrm{O}(4)$ | 1.876(3) |
|  | $\mathrm{O}(12)$ | $2.391(5)$ |  | O (6) | $2.368(5)$ |  | $\mathrm{O}(3)^{\mathrm{i}}$ | $2.426(5)$ | $\mathrm{Mo}(2)$ | $\mathrm{O}(16)^{\mathrm{vii}}$ | $1.739(6)$ |
|  | $\mathrm{O}(13)$ | $2.394(5)$ | Mo(2) | $\mathrm{O}(27)$ | $1.702(6)$ |  | $\mathrm{O}(5)$ | $2.504(6)$ |  | $\mathrm{O}(14)$ | $1.755(6)$ |
|  | $\mathrm{O}(11)$ | $2.475(6)$ |  | $\mathrm{O}(15)^{\text {iii }}$ | 1.737(6) |  | $\mathrm{O}(7)^{\text {ii }}$ | $2.505(6)$ |  | $\mathrm{O}(9)$ | 1.784(5) |
| $\mathrm{Eu}(2)$ | $\mathrm{O}(5)$ | 2.320 (6) |  | $\mathrm{O}(18)^{\text {ii }}$ | 1.811(4) |  | $\mathrm{O}(11)$ | 2.560 (6) |  | $\mathrm{O}(7)$ | 1.794(6) |
|  | $\mathrm{O}(15)$ | 2.327(5) |  | $\mathrm{O}(6)$ | 1.821(4) | Eu(2) | $\mathrm{O}(18)$ | $2.289(6)$ | Mo(3) | $\mathrm{O}(12)$ | 1.731(6) |
|  | $\mathrm{O}(17)$ | $2.389(5)$ | Mo(3) | $\mathrm{O}(22)^{\text {iv }}$ | $1.724(5)$ |  | $\mathrm{O}(15)$ | 2.372(7) |  | $\mathrm{O}(18)^{\text {viii }}$ | 1.740(7) |
|  | $\mathrm{O}(4)$ | $2.396(5)$ |  | $\mathrm{O}(16)^{\text {iii }}$ | $1.725(4)$ |  | $\mathrm{O}(3)^{\mathrm{i}}$ | 2.376 (6) |  | $\mathrm{O}(1)$ | 1.755(6) |
|  | $\mathrm{O}(3)$ | 2.404(5) |  | $\mathrm{O}(12)^{\mathrm{v}}$ | $1.736(5)$ |  | $\mathrm{O}(16)$ | $2.383(6)$ |  | $\mathrm{O}(2)$ | 1.794(6) |
|  | $\mathrm{O}(18)$ | 2.443 (5) |  | $\mathrm{O}(14)$ | 1.860 (6) |  | $\mathrm{O}(11)$ | 2.391 (5) | $\mathrm{Mo}(4)$ | $\mathrm{O}(10)^{\mathrm{ix}}$ | $1.739(6)$ |
|  | $\mathrm{O}(16)$ | $2.462(5)$ | Mo(4) | $\mathrm{O}(19)^{\mathrm{vi}}$ | 1.740(5) |  | $\mathrm{O}(17)$ | 2.447 (7) |  | $\mathrm{O}(8)$ | 1.752(7) |
|  | $\mathrm{O}(2)$ | $2.486(4)$ |  | $\mathrm{O}(1)^{\text {vii }}$ | 1.741(5) |  | $\mathrm{O}(10)$ | 2.463(6) |  | $\mathrm{O}(6)$ | 1.787(5) |
| Eu(3) | $\mathrm{O}(20)$ | $2.350(6)$ |  | $\mathrm{O}(7)^{\mathrm{vi}}$ | $1.763(5)$ |  | $\mathrm{O}(7)^{\mathrm{ii}}$ | 2.532 (6) |  | $\mathrm{O}(11)^{\mathrm{ii}}$ | $1.814(6)$ |
|  | $\mathrm{O}(22)$ | $2.389(5)$ |  | $\mathrm{O}(3)$ | 1.800 (5) | Eu(3) | $\mathrm{O}(19)^{\text {ii }}$ | $2.235(6)$ | Mo(5) | $\mathrm{O}(19)$ | 1.725(7) |
|  | $\mathrm{O}(19)$ | 2.389 (5) | Mo(5) | $\mathrm{O}(13)$ | $1.731(5)$ |  | $\mathrm{O}(1)^{\text {iii }}$ | 2.297(6) |  | $\mathrm{O}(17)^{\text {vii }}$ | 1.727 (7) |
|  | $\mathrm{O}(1)$ | $2.399(4)$ |  | $\mathrm{O}(5)^{\text {i }}$ | 1.735(6) |  | $\mathrm{O}(2)^{\text {iv }}$ | $2.302(6)$ |  | $\mathrm{O}(13)$ | $1.738(6)$ |
|  | $\mathrm{O}(3)$ | 2.400 (5) |  | $\mathrm{O}(10)^{\text {viii }}$ | 1.749(5) |  | $\mathrm{O}(2)^{\mathrm{v}}$ | 2.349 (6) |  | $\mathrm{O}(3)$ | 1.806(5) |
|  | $\mathrm{O}(18)$ | 2.424(4) |  | $\mathrm{O}(26)^{\text {ix }}$ | 1.831(5) |  | $\mathrm{O}(14)$ | $2.436(6)$ |  |  |  |
|  | $\mathrm{O}(2)$ | 2.450 (6) | Mo (6) | $\mathrm{O}(17)^{\mathrm{i}}$ | 1.730 (5) |  | $\mathrm{O}(20)^{\mathrm{vi}}$ | 2.477 (6) | $\mathrm{Eu}(1)$ | $\mathrm{Eu}(2)$ | 3.7168(6) |
|  | $\mathrm{O}(23)$ | $2.491(5)$ |  | $\mathrm{O}(4)^{\text {iii }}$ | 1.746(5) |  | $\mathrm{O}(8)^{\text {iii }}$ | 2.483 (6) | Eu(3) | $\mathrm{Eu}(3)^{\mathrm{x}}$ | 3.6297 (8) |
| $\mathrm{Eu}(4)$ | O (7) | 2.282(6) |  | $\mathrm{O}(20)^{\text {iv }}$ | 1.755(6) |  |  |  |  |  |  |
|  | $\mathrm{O}(8)$ | $2.337(5)$ |  | $\mathrm{O}(11)$ | 1.797(5) |  |  |  |  |  |  |
|  | $\mathrm{O}(26)^{\mathrm{i}}$ | $2.341(5)$ | Mo(7) | $\mathrm{O}(9)^{\mathrm{x}}$ | 1.741(6) |  |  |  |  |  |  |
|  | $\mathrm{O}(21)$ | $2.344(5)$ |  | $\mathrm{O}(21)$ | 1.742(5) |  |  |  |  |  |  |
|  | $\mathrm{O}(24)$ | $2.395(4)$ |  | $\mathrm{O}(8)^{\text {ii }}$ | 1.745(5) |  |  |  |  |  |  |
|  | $\mathrm{O}(25)^{\mathrm{i}}$ | $2.412(5)$ |  | $\mathrm{O}(2)$ | $1.786(5)$ |  |  |  |  |  |  |
|  | $\mathrm{O}(11)^{\mathrm{i}}$ | 2.458(4) |  |  |  |  |  |  |  |  |  |
|  |  |  | $\mathrm{Eu}(1)$ | $\mathrm{Eu}(4)^{\mathbf{i}}$ | 3.6681(5) |  |  |  |  |  |  |
|  |  |  | $\mathrm{Eu}(2)$ | $\mathrm{Eu}(3)$ | $3.6615(5)$ |  |  |  |  |  |  |

Note. Symmetry codes for $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ : (i) $\frac{1}{2}-x, \frac{3}{2}-y$, $-z$; (ii) $1-x, y, \frac{1}{2}-z$; (iii) $-\frac{1}{2}+x, \frac{3}{2}-y, \frac{1}{2}+z$; (iv) $-\frac{1}{2}+x,-\frac{1}{2}+y, z$; (v) $\frac{1}{2}-x,-\frac{1}{2}+y$, $\frac{1}{2}-z$; (vi) $1-x, 2-y,-z$; (vii) $x, 2-y,-\frac{1}{2}+z$; (viii) $-x, y, \frac{1}{2}-z$; (ix) $-x, 2-y,-z$; (x) $\frac{1}{2}+x,-\frac{1}{2}+y, z$.
Symmetry codes for $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ : (i) $\frac{3}{2}-x, \frac{3}{2}-y, 1-z$; (ii) $1-x, y$, $\frac{3}{2}-z$; (iii) $-\frac{1}{2}+x, \frac{1}{2}+y, z ;$ (iv) $\frac{3}{2}-x, \frac{1}{2}+y, \frac{3}{2}-z ;$ (v) $-\frac{1}{2}+x, \frac{3}{2}+y, \frac{1}{2}+z$; (vi) $\frac{3}{2}-x, \frac{3}{2}-y, 2-z$; (vii) $\frac{1}{2}+x, \frac{3}{2}-y, \frac{1}{2}+z$; (viii) $1-x, 1-y, 1-z$; (ix) $x, 1-y, \frac{1}{2}+x$; (x) $1-x, 2-y, 2-z$.
$900.6 \mathrm{vs}(\mathrm{sh}), 872.6 \mathrm{vs}, ~ 841.8 \mathrm{~s}, ~ 823.5 \mathrm{~s}, 784.9 \mathrm{vs}(\mathrm{br}), 753.1 \mathrm{~s}$, $743.4 \mathrm{~s}, 729.9 \mathrm{~s}, 717.4 \mathrm{~s}, 418.5 \mathrm{~m} \mathrm{~cm}^{-1}$.

A slow cooling ( $3^{\circ} \mathrm{C} \mathrm{min}^{-1}$ ) of the sample yielded completely different products, consisting of $\beta^{\prime}-\mathrm{Eu}_{2}\left(\mathrm{MoO}_{4}\right)_{3}$ and unknown phases.

## Preparation of $E u_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$

$\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ can be obtained under the same conditions as $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ (Fig. 1c), but in lower reproducibility. We established a reproducible synthesis procedure as follows. The firing of a mixture ( 100 mg ) of $\mathrm{Eu}_{2} \mathrm{O}_{3}$ and $\mathrm{MoO}_{3}$ in a $2: 7$ molar ratio at $800^{\circ} \mathrm{C}$ for 2 h yielded an assembly of small crystals of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$. Successful crystal growth was achieved by heating the product $(20 \mathrm{mg})$ mixed with $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}(20 \mathrm{mg})$ at $800^{\circ} \mathrm{C}$ for 2 h (Fig.

1d). IR spectrum; $968.1 \mathrm{~m}(\mathrm{sh}), 929.5 \mathrm{~s}(\mathrm{sh}), 910.2 \mathrm{~s}, 875.5 \mathrm{vs}$, $834.1 \mathrm{vs}, 797.4 \mathrm{vs}, 779.4 \mathrm{vs}, 744.4 \mathrm{~s}, 724.1 \mathrm{~s}, 442.6 \mathrm{~m} \mathrm{~cm}^{-1}$.

## X-Ray Crystallographic Analyses

The single-crystal X-ray structural analyses were carried out for $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ using a Rigaku RAXIS-RAPID imaging-plate X-ray diffractometer and the structure analysis software package TEXSAN (10). Structures of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ were solved by SHELXS-86 (11) and SIR92 (12) respectively, and refined with full-matrix least-squares techniques. Numerical absorption corrections were done using SHAPE (13) and NUMABS (14). All atoms were refined anisotropically. The complete measurement conditions and results of the refinements are summarized in Table 1. Atomic coordinates and


FIG. 2. The structure of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ viewed down the $c$ axis. The $\left\{\mathrm{MoO}_{4}\right\}$ and $\left\{\mathrm{MoO}_{5}\right\}$ units are represented polyhedrally. Eu atoms are denoted by gray spheres.
selected bond distances are listed in Tables 2 and 3, respectively. The negative residual difference Fourier peaks were considerably large, 7.2 and $-5.8 \mathrm{e}^{-3}$ for $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ respectively, due to poor quality of the single crystals used and/or incomplete absorption correction. Further details of the crystal structure data can be ordered from Fachinformationszentrum Karlsruhe, 76344 EggensteinLeopoldshafen (http://www.fiz-karlsruhe.de), under the depository numbers CSD-411960 $\left(\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}\right)$ and CSD$411961\left(\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}\right)$.

## Spectroscopies

Contents of Mo and Eu were analyzed by a X-ray fluorescence spectrometer (JEOL JSX-3200). IR spectra were measured by the KBr-disk method on a JASCO FT/IR-410 spectrometer.

## RESULTS AND DISCUSSION

Formations of $E u_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $E u_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$
If we assume that the $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ precursor is completely transformed to $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ or $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$, the reactions are described as follows.

$$
\begin{gather*}
2\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27} \\
+9 \mathrm{MoO}_{3}+36 \mathrm{H}_{2} \mathrm{O}  \tag{1}\\
3\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39} \\
+14 \mathrm{MoO}_{3}+54 \mathrm{H}_{2} \mathrm{O} . \tag{2}
\end{gather*}
$$

The $\mathrm{MoO}_{3}$ released from the sample recrystallized in the quartz tube of the furnace. The calculated weight losses for the Eqs. [1] and [2] are 53.2 and $54.5 \%$, respectively. However, the main product was the $\mathrm{Eu}_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$ melt, and the observed weight loss was only $36 \%$, indicating that the $\mathrm{MoO}_{3}$ content in the melt is much larger than those in $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}\left(=\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 3.5 \mathrm{MoO}_{3}\right)$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ $\left(=\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 3.33 \mathrm{MoO}_{3}\right)$. The elemental analysis of the melt showed to have a composition $\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 6.1 \mathrm{MoO}_{3}$. The composition of the melt formed by heating the $\mathrm{Eu}_{2} \mathrm{O}_{3}+8 \mathrm{MoO}_{3}$ mixture at $800^{\circ} \mathrm{C}$ was slightly $\mathrm{MoO}_{3}$-rich $\left(\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 6.5 \mathrm{MoO}_{3}\right)$. Powder X-ray diffraction patterns revealed that all these melts are amorphous, being in a glass


FIG. 3. Views of (a) $\left\{\mathrm{Mo}_{3} \mathrm{O}_{11}\right\}$, (b) $\left\{\mathrm{Eu}_{2} \mathrm{O}_{12}\right\}$, and (c) $\left\{\mathrm{Eu}_{2} \mathrm{O}_{13}\right\}$ groups in $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$. The symmetry operations are listed in Table 3 .


FIG. 4. The structure of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ viewed down the $c$ axis. The $\left\{\mathrm{MoO}_{4}\right\}$ units are represented polyhedrally. Eu atoms are denoted by gray spheres.
state after cooling. It should be noted that the IR spectrum of the $\mathrm{Eu}_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$ glass ( $962 \mathrm{~m}(\mathrm{sh}), 962 \mathrm{~s}(\mathrm{sh}), 891.9 \mathrm{vs}(\mathrm{br})$, $\left.876.5 \mathrm{vs}(\mathrm{br}), 789 \mathrm{~s}(\mathrm{br}), 759 \mathrm{~s}(\mathrm{sh}) \mathrm{cm}^{-1}\right)$ is similar to that of stoichiometric compounds $R_{2} \mathrm{O}_{3} \cdot 6 \mathrm{MoO}_{3} \quad(R=\mathrm{La}-\mathrm{Gd})$ (15). Since melting points of the stoichiometric $R_{2} \mathrm{O}_{3}$. $6 \mathrm{MoO}_{3}$ are in the range $680-745^{\circ} \mathrm{C}(15)$, the amorphous $\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 6.1 \mathrm{MoO}_{3}$ and $\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 6.5 \mathrm{MoO}_{3}$ glass phases were formed as a result of the rapid cooling from their liquid states at $800^{\circ} \mathrm{C}$.

As described under Experimental, reuse of the same alumina container were effective in enhancing crystallization of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$, suggesting that nucleation occurred gradually on the surface of the container through the repeated exposure to the $\mathrm{Eu}_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$ melt. This is supported by the successful crystal growth of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ in the $\mathrm{Eu}_{2} \mathrm{O}_{3}-\mathrm{MoO}_{3}$ melt using the seed-crystal technique (Figs. 1b and 1d). These results indicate that $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ were formed not directly from the decomposition of $\left[\mathrm{Eu}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{12} \mathrm{Mo}_{8} \mathrm{O}_{27}\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (or reaction of $\mathrm{Eu}_{2} \mathrm{O}_{3}+$ $8 \mathrm{MoO}_{3}$ ), but via the melt of $\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 6.1 \mathrm{MoO}_{3}$ (or $\mathrm{Eu}_{2} \mathrm{O}_{3} \cdot 6.5 \mathrm{MoO}_{3}$ ). On the other hand, the formation of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ by firing the $2 \mathrm{Eu}_{2} \mathrm{O}_{3}+7 \mathrm{MoO}_{3}$ mixture seems to be a direct solid reaction (with loss of $\mathrm{MoO}_{3}$ ), because no glassy substance coexisted in the product.

Stoichiometric syntheses excluding the evaporation of $\mathrm{MoO}_{3}$ have been attempted by the use of evacuated quartz ampoules, in which stoichiometric mixtures of oxides $\left(\mathrm{Eu}_{2} \mathrm{O}_{3}: \mathrm{MoO}_{3}=2: 7\right.$ and $\left.3: 10\right)$ were heated at $800^{\circ} \mathrm{C}$ for 2 h . However, no $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ nor $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ have been obtained by this procedure. Reaction of $2 \mathrm{Eu}_{2} \mathrm{O}_{3}+7 \mathrm{MoO}_{3}$ at higher temperature $\left(1000^{\circ} \mathrm{C}\right)$ in the ampoule gave a mixture of transparent crystals and colored powders. The former compound exhibits an IR spectrum completely different from those of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ and $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$. X-ray
structural analysis for this product revealed it to be $\beta^{\prime}-\mathrm{Eu}_{2}\left(\mathrm{MoO}_{4}\right)_{3}$, which is isostructural with Gd analogue (see Introduction).

## Structure of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$

Figure 2 shows the structure of $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ viewed down the $c$ axis. $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$ can be best described as a layer compound, consisting of $\left\{\mathrm{MoO}_{4}\right\}$ - and $\left\{\mathrm{Mo}_{3} \mathrm{O}_{11}\right\}$-containing layers and interstitial $\{\mathrm{Eu}\}$ layers parallel to the $b c$ plane. The $\left\{\mathrm{Mo}_{3} \mathrm{O}_{11}\right\}$ group is constructed of a distorted $\mathrm{Mo}(1) \mathrm{O}_{5}$ trigonal bipyramid and corner-sharing $\mathrm{Mo}(2) \mathrm{O}_{4}$ and $\mathrm{Mo}(3) \mathrm{O}_{4}$ tetrahedra (Fig. 3a). Such a trimeric molybdate group is the first example among all other structurally characterized rare-earth molybdates where one finds


FIG. 5. Views of (a) $\left\{\mathrm{Mo}_{2} \mathrm{O}_{7}\right\}$, (b) $\left\{\mathrm{Eu}_{2} \mathrm{O}_{13}\right\}$, and (c) $\left\{\mathrm{Eu}_{2} \mathrm{O}_{12}\right\}$ groups in $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$. The symmetry operations: (xi) $2-x, y, \frac{3}{2}-z$. Other symmetry operations are listed in Table 3.


FIG. 6. The structures of (a) $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ and (b) $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ viewed down the $a$ axes. The single layer $A$ and $B$ projected on to the ( 001 ) planes are presented in (c) and (d). The $\left\{\mathrm{Mo}_{2} \mathrm{O}_{7}\right\}$ groups are plotted by hatched polyhedra, and Eu and Ce atoms are denoted by gray spheres. The crystallographic twofold and twofold screw axes and inversion centers are also shown in (c) and (d). The arrow in (a) corresponds to the $+b$ direction in (c) (see text).
monomeric $\left\{\mathrm{MoO}_{4}\right\}$ in $R_{2} \mathrm{MoO}_{6}(R=\mathrm{La}, \mathrm{Tb})$ (3) and $\mathrm{La}_{2}\left(\mathrm{MoO}_{4}\right)_{3}$ (16), dimeric $\left\{\mathrm{Mo}_{2} \mathrm{O}_{7}\right\}$ in $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ (8), tetrameric $\left\{\mathrm{Mo}_{4} \mathrm{O}_{15}\right\}$ in $\mathrm{Ho}_{2} \mathrm{Mo}_{4} \mathrm{O}_{15}$ (17), and polymeric $\left\{\mathrm{Mo}_{2} \mathrm{O}_{7}\right\}_{\infty}$ in $R_{2} \mathrm{Mo}_{4} \mathrm{O}_{15}(R=\mathrm{Ce}, \mathrm{Pr})(18,19)$. The axial $\mathrm{Mo}(1)-\mathrm{O}(6)$ bond distance $(2.368(5) \AA)$ in the $\mathrm{Mo}(1) \mathrm{O}_{5}$ polyhedron is much longer than the opposite axial $\mathrm{Mo}(1)-\mathrm{O}(24)$ bond length ( $1.726(5) \AA$ ). All other $\operatorname{Mo}(4), \operatorname{Mo}(5), \operatorname{Mo}(6)$, and $\mathrm{Mo}(7)$ atoms from discrete $\mathrm{MoO}_{4}$ tetrahedra, which exhibit double $\left\{\mathrm{MoO}_{4}\right\}$ layers in the lattice (Fig. 2). Each of the $\mathrm{Eu}(1), \mathrm{Eu}(2)$, and $\mathrm{Eu}(3)$ atoms is surrounded by O atoms ( $<2.7 \AA$ ) with a distorted square-antiprismatic coordination. These distortions are considerable compared with the
nearly ideal square-antiprismatic geometries of the $\mathrm{RO}_{8}$ sites in polyoxomolybdates, $\left[R\left(\mathrm{Mo}_{8} \mathrm{O}_{26}\right)_{2}\right]^{5-}(R=\mathrm{La})(20)$ and $\left[R\left(X \mathrm{Mo}_{11} \mathrm{O}_{39}\right)_{2}\right]^{13-}(R=\mathrm{Nd}$, $\operatorname{Pr} ; X=\mathrm{Ge}, \mathrm{Si})(21)$. The Eu(4) atom achieves sevenfold coordination ( $<2.7 \AA$ ) by O atoms with an approximate monocapped trigonal prism. The $\mathrm{Eu}(1) \mathrm{O}_{8}$ and $\mathrm{Eu}(4)^{\mathrm{i}} \mathrm{O}_{7}$ polyhedra share the face defined by the $\mathrm{O}(11), \mathrm{O}(25)$, and $\mathrm{O}(26)$ atoms (Fig. 3b). Similarly, the $\mathrm{Eu}(2) \mathrm{O}_{8}$ and $\mathrm{Eu}(3) \mathrm{O}_{8}$ polyhedra share the face defined by the $\mathrm{O}(2), \mathrm{O}(3)$, and $\mathrm{O}(18)$ atoms (Fig. 3c). These face-sharings of the $\mathrm{EuO}_{n}$ polyhedra result in short $\mathrm{Eu}(1) \cdots \mathrm{Eu}(4)^{\mathrm{i}}(3.6681(5) \AA)$ and $\mathrm{Eu}(2) \cdots \operatorname{Eu}(3)(3.6615(5) \AA)$ separations.

## Structure of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ and Comparison with $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$

Unlike $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}$, the structure of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ exhibits a three-dimensional network of molybdate groups and Eu atoms. Figure 4 represents a packing diagram of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ viewed down the $c$ axis. All of the Mo atoms form $\mathrm{MoO}_{4}$ tetrahedra, of which $\mathrm{Mo}(1) \mathrm{O}_{4}$ is connected with the symmetry-related $\mathrm{Mo}(1)^{\mathrm{x}} \mathrm{O}_{4}$ through the $\mathrm{O}(4)$ atom, to form a $\left\{\mathrm{Mo}_{2} \mathrm{O}_{7}\right\}$ group (Fig. 5a). Other $\mathrm{MoO}_{4}$ tetrahedra are discrete. Each of the $\mathrm{Eu}(1)$ and $\mathrm{Eu}(2)$ atoms is squareantiprismatically coordinated by eight O atoms ( $<2.7 \AA$ ). The $\mathrm{Eu}(1) \mathrm{O}_{8}$ and $\mathrm{Eu}(2) \mathrm{O}_{8}$ polyhedra are face-shared through the $\mathrm{O}(11), \mathrm{O}(3)^{\mathrm{i}}$, and $\mathrm{O}(7)$ atoms with a short ( $3.7168 \AA$ ) $\mathrm{Eu}(1) \cdots \mathrm{Eu}(2)$ separation (Fig. 5b). Seven O atoms coordinate to the $\mathrm{Eu}(3)$ atom ( $<2.7 \AA$ ), to give a $\mathrm{Eu}(3) \mathrm{O}_{7}$ polyhedron. The $\mathrm{Eu}(3) \mathrm{O}_{7}$ and symmetry-related $\mathrm{Eu}(3)^{\mathrm{x}} \mathrm{O}_{7}$ polyhedra share the $\mathrm{O}(2)^{\mathrm{iv}} \cdots \mathrm{O}(2)^{\mathrm{v}}$ edge with a short $\left(3.6297(8) \AA\right.$ ) $\operatorname{Eu}(3) \cdots E u(3)^{x}$ separation (Fig. 5c).

The structure of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ is closely related to the previously reported $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ (8). The two compounds, which crystallize in different space groups ( $P \overline{1}$ and $C 2 / c$, respectively), are compared in Fig. 6. For convenience, the original axes of $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ have been transformed by the matrix $\left[a^{\prime}=-a+c ; \quad b^{\prime}=a+b+c ; \quad c^{\prime}=-a / 2+\right.$ $b / 2-c / 2$ ] (new cell constants: $a=12.428, b=19.73$, $c=13.998 \AA, \alpha=77.7, \beta=85.3, \gamma=88.66^{\circ}$ ) to be adjusted to the axes of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$. Structures of $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ and $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ viewed along the $a$ axes are shown in Figs. 6a and 6 b respectively, where similar layers, denoted by $A$ and $B$, are stacked in the $c$ direction. Single layers $A$ and $B$ are compared in Figs. 6c and 6d respectively, where small shifts and/or rotations of the $\mathrm{MoO}_{4}$ tetrahedra and $R$ atoms are observed. The layer $A$ possesses crystallographic twofold rotational and twofold screw axes parallel to the $b$ axis, while the layer $B$ has only inversion centers. Also, the $+b$ and $-b$ directions are unequivalent (anisotropic) for the single layer $A(+b$ was denoted by an arrow in Fig. 6c), but are isotropic for the single layer $B$. The stacking of the layers are also different in the two compounds: the layers $A$ are stacked with alternate directions (up and down arrows in Fig. 6a), while the layers $B$ are stacked with glinding in the $a b$ plane (Fig. 6b). The structural difference between $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ and $\mathrm{Ce}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$ may be due to the difference in the ionic radius of $\mathrm{Eu}^{3+}$ and $\mathrm{Ce}^{3+}$.

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[^1]:    ${ }^{a} R_{1}=\sum\left\|F_{\mathrm{o}}\left|-\left|F_{\mathrm{c}} \| / \sum\right| F_{\mathrm{o}}\right|\right.$ for $I>2 \sigma(I)$.
    ${ }^{b} \mathrm{w} R_{2}=\left\{\Sigma\left[\mathrm{w}\left(F_{\mathrm{o}}^{2}-F_{\mathrm{c}}^{2}\right)^{2}\right] / \Sigma\left[\mathrm{w}\left(F_{\mathrm{o}}^{2}\right)^{2}\right]\right\}^{1 / 2}$, where $\mathrm{w}=\left[\sigma_{\mathrm{c}}^{2}\left(F_{\mathrm{o}}^{2}\right)+\right.$ $\left.\left.p\left(\operatorname{Max}\left(F_{\mathrm{o}}^{2}, 0\right)+2 F_{\mathrm{c}}^{2}\right) / 3\right\}^{2}\right]^{-1}, \quad p=0.01$ for $\mathrm{Eu}_{4} \mathrm{Mo}_{7} \mathrm{O}_{27}, p=0.05$ for $\mathrm{Eu}_{6} \mathrm{Mo}_{10} \mathrm{O}_{39}$.

